

**AMENDMENTS TO THE CLAIMS**

The listing of the claims will replace all prior versions, and listings, of claims:

**LISTING OF CLAIMS:**

Claims 1-38 (canceled)

Claim 39 (original): A method of multivariate spectral analysis, comprising the steps of:

a) obtaining an estimate of spectral error covariance  $\mathbf{E}_A$  for measured set of multivariate spectral data  $\mathbf{A}$ ;

b) decomposing the spectral error covariance  $\mathbf{E}_A$  according to  $\mathbf{E}_A = \mathbf{TP} + \mathbf{E}$ , where  $\mathbf{T}$  is a set of  $n \times r$  scores and  $\mathbf{P}$  is a set of  $r \times p$  loading vectors obtained from factor analysis of the spectral error covariance  $\mathbf{E}_A$ , and  $\mathbf{E}$  is a set of  $n \times p$  random errors and spectral variations not useful for prediction;

c) guessing pure-component spectra  $\mathbf{K}$  for the set of multivariate spectral data  $\mathbf{A}$ ;

d) predicting a set of component values  $\hat{\mathbf{C}}$  according to

$$\hat{\mathbf{C}} = \mathbf{AK}^T(\mathbf{KK}^T)^{-1} = \mathbf{A}(\mathbf{K}^T)^+;$$

e) augmenting the set of predicted component values  $\hat{\mathbf{C}}$  with at least one vector of the  $\mathbf{T}$  scores to obtain a first set of augmented component values  $\hat{\hat{\mathbf{C}}}$ ;

f) estimating augmented pure-component spectra  $\hat{\hat{\mathbf{K}}}$  according to

$$\hat{\hat{\mathbf{K}}} = (\hat{\hat{\mathbf{C}}}^T \hat{\hat{\mathbf{C}}})^{-1} \hat{\hat{\mathbf{C}}}^T \mathbf{A} = \hat{\hat{\mathbf{C}}}^+ \mathbf{A};$$

g) testing for convergence according to  $\left\| \mathbf{A} - \hat{\hat{\mathbf{C}}} \hat{\hat{\mathbf{K}}} \right\|^2$ ;

h) predicting a second set of augmented component values  $\hat{\hat{\hat{\mathbf{C}}}}$  according to

$$\hat{\hat{\hat{\mathbf{C}}}} = \mathbf{A} \hat{\hat{\mathbf{K}}}^T (\hat{\hat{\mathbf{K}}} \hat{\hat{\mathbf{K}}}^T)^{-1} = \mathbf{A} (\hat{\hat{\mathbf{K}}}^T)^+;$$

i) replacing the augmented portion of the second set of augmented component values  $\hat{\hat{\mathbf{C}}}$  with the at least one vector of the  $\mathbf{T}$  scores to obtain a third set of augmented component values  $\hat{\hat{\hat{\mathbf{C}}}}$ ; and

j) repeating steps f) through i) at least once.

Claim 40 (original): The method of Claim 39, wherein the steps f) through i) are repeated until the test of step g) converges to obtain an alternating classical least squares solution for  $\hat{\mathbf{K}}$  and  $\hat{\mathbf{C}}$ .

Claim 41 (original): The method of Claim 39, further comprising replacing the augmented portion of the augmented pure-component spectra  $\hat{\mathbf{K}}$  with at least one vector of the  $\mathbf{P}$  loading vectors prior to step h).

Claim 42 (original): The method of Claim 39, further comprising augmenting  $\hat{\mathbf{K}}$  with at least one vector representing a spectral shape that is representative of at least one additional source of spectral variation prior to step h).

Claim 43 (original): The method of Claim 39, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{K}}$  at step f).

Claim 44 (original): The method of Claim 43, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 45 (original): The method of Claim 39, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{C}}$  at step h).

Claim 46 (original): The method of Claim 45, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 47 (original): The method of Claim 39, wherein the guessed pure-component spectra  $\mathbf{K}$  comprises random numbers.

Claim 48 (original): The method of Claim 39, wherein the measured set of multivariate spectral data  $\mathbf{A}$  comprises image data.

Claim 49 (original): The method of Claim 48, wherein the spectral error covariance  $\mathbf{E}_A$  is obtained from a shift difference generated from a single image.

Claim 50 (original): The method of Claim 48, wherein the spectral error covariance  $E_A$  is obtained from repeat image spectra.

Claim 51 (original): A method of multivariate spectral analysis, comprising the steps of:

- a) obtaining an estimate of spectral error covariance  $E_A$  for measured set of multivariate spectral data  $A$ ;
- b) decomposing the spectral error covariance  $E_A$  according to  $E_A = TP + E$ , where  $T$  is a set of  $n \times r$  scores and  $P$  is a set of  $r \times p$  loading vectors obtained from factor analysis of the spectral error covariance  $E_A$ , and  $E$  is a set of  $n \times p$  random errors and spectral variations not useful for prediction;
- c) guessing pure-component spectra  $K$  for the set of multivariate spectral data  $A$ ;
- d) augmenting the pure-component spectra  $K$  with at least one vector of the  $P$  loading vectors to obtain first augmented pure-component spectra  $\tilde{K}$ ;
- e) predicting a first set of augmented component values  $\hat{\tilde{C}}$  according to
 
$$\hat{\tilde{C}} = A\tilde{K}^T(\tilde{K}\tilde{K}^T)^{-1} = A(\tilde{K}^T)^+;$$
- f) estimating second augmented pure-component spectra  $\hat{\tilde{K}}$  according to
 
$$\hat{\tilde{K}} = (\hat{\tilde{C}}^T\hat{\tilde{C}})^{-1}\hat{\tilde{C}}^T A = \hat{\tilde{C}}^+ A;$$
- g) testing for convergence according to  $\|A - \hat{\tilde{C}}\hat{\tilde{K}}\|^2$ ;
- h) replacing the augmented portion of the second augmented pure-component spectra  $\hat{\tilde{K}}$  with the at least one vector of the  $P$  loading vectors to obtain third augmented pure-component spectra  $\hat{\tilde{K}}$ ; and
- i) predicting a second set of augmented component values  $\hat{\tilde{C}}$  according to
 
$$\hat{\tilde{C}} = A\hat{\tilde{K}}^T(\hat{\tilde{K}}\hat{\tilde{K}}^T)^{-1} = A(\hat{\tilde{K}}^T)^+;$$
- j) repeating steps f) through i) at least once.

Claim 52 (original): The method of Claim 51, wherein the steps f) through i) are repeated until the test of step g) converges to obtain an alternating classical least squares solution for  $\hat{\mathbf{K}}$  and  $\hat{\mathbf{C}}$ .

Claim 53 (original): The method of Claim 51, further comprising replacing the augmented portion of the set of augmented component values  $\hat{\mathbf{C}}$  with at least one vector of the  $\mathbf{T}$  scores prior to step h).

Claim 54 (original): The method of Claim 51, further comprising augmenting  $\hat{\mathbf{K}}$  with at least one vector representing a spectral shape that is representative of at least one additional source of spectral variation prior to step h).

Claim 55 (original): The method of Claim 51, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{K}}$  at step f).

Claim 56 (original): The method of Claim 55, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 57 (original): The method of Claim 51, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{C}}$  at step h).

Claim 58 (original): The method of Claim 57, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 59 (original): The method of Claim 51, wherein the guessed pure-component spectra  $\mathbf{K}$  comprises random numbers.

Claim 60 (original): The method of Claim 51, wherein the measured set of multivariate spectral data  $\mathbf{A}$  comprises image data.

Claim 61 (original): The method of Claim 60, wherein the estimate of the error covariance  $\mathbf{E}_A$  is obtained from a shift difference generated from a single image.

Claim 62 (original): The method of Claim 60, wherein the estimate of the error covariance  $E_A$  is obtained from repeat image spectra.

Claim 63 (original): A method of multivariate spectral analysis, comprising the steps of:

a) obtaining an estimate of the spectral error covariance  $E_A$  for measured set of multivariate spectral data  $A$ ;

b) decomposing the spectral error covariance  $E_A$  according to  $E_A = TP + E$ , where  $T$  is a set of  $n \times r$  scores and  $P$  is a set of  $r \times p$  loading vectors obtained from factor analysis of the spectral error covariance  $E_A$ , and  $E$  is a set of  $n \times p$  random errors and spectral variations not useful for prediction;

c) guessing a set of component values  $C$  for the set of multivariate spectral data  $A$ ;

d) estimating pure-component spectra  $\hat{K}$  according to  $\hat{K} = (C^T C)^{-1} C^T A = C^+ A$ ;

e) augmenting the pure-component spectra  $\hat{K}$  with at least one vector of the  $P$  loading vectors to obtain first augmented pure-component spectra  $\hat{\hat{K}}$ ;

f) predicting a first set of augmented component values  $\hat{\hat{C}}$  according to  $\hat{\hat{C}} = A \hat{\hat{K}}^T (\hat{\hat{K}} \hat{\hat{K}}^T)^{-1} = A (\hat{\hat{K}}^T)^+$ ;

g) testing for convergence according to  $\|A - \hat{\hat{C}} \hat{\hat{K}}\|^2$ ;

h) estimating second augmented pure-component spectra  $\hat{\hat{K}}$  according to  $\hat{\hat{K}} = (\hat{\hat{C}}^T \hat{\hat{C}})^{-1} \hat{\hat{C}}^T A = \hat{\hat{C}}^+ A$ ;

i) replacing the augmented portion of the second augmented pure-component spectra  $\hat{\hat{K}}$  with the at least one vector of the  $P$  loading vectors to obtain a third augmented pure-component spectra  $\hat{\hat{K}}$  and

j) repeating steps f) through i) at least once.

Claim 64 (original): The method of Claim 63, wherein the steps f) through i) are repeated until the test of step g) converges to obtain an alternating classical least squares solution for  $\hat{\hat{K}}$  and  $\hat{\hat{C}}$ .

Claim 65 (original): The method of Claim 63, further comprising replacing the augmented portion of the set of augmented component values  $\hat{\mathbf{C}}$  with at least one vector of the  $\mathbf{T}$  scores prior to step h).

Claim 66 (original): The method of Claim 63, further comprising augmenting  $\hat{\mathbf{K}}$  with at least one vector representing a spectral shape that is representative of at least one additional source of spectral variation prior to step h).

Claim 67 (original): The method of Claim 63, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{K}}$  at step h).

Claim 68 (original): The method of Claim 67, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 69 (original): The method of Claim 63, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{C}}$  at step f).

Claim 70 (original): The method of Claim 69, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 71 (original): The method of Claim 63, wherein the guessed set of component values  $\mathbf{C}$  comprises random numbers.

Claim 72 (original): The method of Claim 52, wherein the measured set of multivariate spectral data  $\mathbf{A}$  comprises image data.

Claim 73 (original): The method of Claim 62, wherein the spectral error covariance  $\mathbf{E}_A$  is obtained from a shift difference generated from a single image.

Claim 74 (original): The method of Claim 62, wherein the spectral error covariance  $\mathbf{E}_A$  is obtained from repeat image spectra.

Claim 75 (original): A method of multivariate spectral analysis, comprising the steps of:

- a) obtaining an estimate of the spectral error covariance  $\mathbf{E}_A$  for measured set of multivariate spectral data  $\mathbf{A}$ ;
- b) decomposing the spectral error covariance  $\mathbf{E}_A$  according to  $\mathbf{E}_A = \mathbf{T}\mathbf{P} + \mathbf{E}$ , where  $\mathbf{T}$  is a set of  $n \times r$  scores and  $\mathbf{P}$  is a set of  $r \times p$  loading vectors obtained from factor analysis of the spectral error covariance  $\mathbf{E}_A$ , and  $\mathbf{E}$  is a set of  $n \times p$  random errors and spectral variations not useful for prediction;
- c) guessing a set of component values  $\mathbf{C}$  for the set of multivariate spectral data  $\mathbf{A}$ ;
- d) augmenting the set of component values  $\mathbf{C}$  with at least one vector of the  $\mathbf{T}$  scores to obtain a first set of augmented component values  $\tilde{\mathbf{C}}$ ;
- e) estimating augmented pure-component spectra  $\hat{\mathbf{K}}$  according to 
$$\hat{\mathbf{K}} = (\tilde{\mathbf{C}}^T \tilde{\mathbf{C}})^{-1} \tilde{\mathbf{C}}^T \mathbf{A} = \tilde{\mathbf{C}}^+ \mathbf{A};$$
- f) testing for convergence according to  $\|\mathbf{A} - \tilde{\mathbf{C}}\hat{\mathbf{K}}\|^2$ ;
- g) predicting a second set of augmented component values  $\hat{\tilde{\mathbf{C}}}$  according to 
$$\hat{\tilde{\mathbf{C}}} = \mathbf{A}\hat{\mathbf{K}}^T(\hat{\mathbf{K}}\hat{\mathbf{K}}^T)^{-1} = \mathbf{A}(\hat{\mathbf{K}}^T)^+;$$
- h) replacing the augmented portion of the second set of augmented component values  $\hat{\tilde{\mathbf{C}}}$  with the at least one vector of the  $\mathbf{T}$  scores to obtain a third set of augmented component values  $\hat{\hat{\mathbf{C}}}$  and
- i) repeating steps e) through h) at least once, using the augmented component values  $\hat{\hat{\mathbf{C}}}$  in step f).

Claim 76 (original): The method of Claim 75, wherein the steps e) through h) are repeated until the test of step g) converges to obtain an alternating classical least squares solution for  $\hat{\mathbf{K}}$  and  $\hat{\tilde{\mathbf{C}}}$ .

Claim 77 (original): The method of Claim 75, further comprising replacing the augmented portion of the augmented pure-component spectra  $\hat{\mathbf{K}}$  with at least one vector of the  $\mathbf{P}$  loading vectors prior to step e).

Claim 78 (original): The method of Claim 75, further comprising augmenting  $\hat{\mathbf{K}}$  with at least one vector representing a spectral shape that is representative of at least one additional source of spectral variation prior to step e).

Claim 79 (original): The method of Claim 75, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{K}}$  at step e).

Claim 80 (original): The method of Claim 79, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 81 (original): The method of Claim 75, further comprising applying at least one constraint to the non-augmented portion of  $\hat{\mathbf{C}}$  at step g).

Claim 82 (original): The method of Claim 81, wherein the at least one constraint is selected from the group consisting of non-negativity, equality, closure, monotonic constraint, unimodality, and selectivity.

Claim 83 (original): The method of Claim 75, wherein the guessed set of component values  $\mathbf{C}$  comprises random numbers.

Claim 84 (original): The method of Claim 75, wherein the measured set of multivariate spectral data  $\mathbf{A}$  comprises image data.

Claim 85 (original): The method of Claim 84, wherein the spectral error covariance  $\mathbf{E}_A$  is obtained from a shift difference generated from a single image.

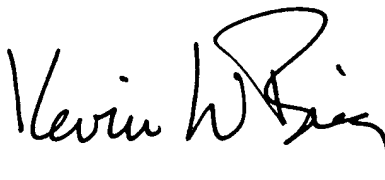
Claim 86 (original): The method of Claim 84, wherein the spectral error covariance  $\mathbf{E}_A$  is obtained from repeat image spectra.



**CONCLUSION**

Applicants have canceled the nonelected claims and urge that the application is now in condition for allowance.

Respectfully submitted,



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**CERTIFICATION UNDER 37 CFR 1.8**

I hereby certify that this correspondence and documents referred to herein were deposited with the United States Postal Service as first class mail addressed to: Commissioner for Patents, Alexandria, VA 22313-1450 on the date shown below.

Date: 7/13/04

By: Martha Inzillo